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# Analysis of reporting behavior using the **hopit** R-package (v0.11.5)

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#### Abstract

Self-reported health, happiness, attitudes, and other statuses or perceptions are often the subject of biases that may come from different sources. For example, the evaluation of an individual's own health may depend on previous medical diagnoses, functional status, and symptoms and signs of illness; as on well as life-style behaviors, including contextual social, gender, agespecific, linguistic and other cultural factors (Jylha 2009; Oksuzyan et al. 2019). The hopit package offers versatile functions for analyzing different self-reported ordinal variables, and for helping to estimate their biases. Specifically, the package provides the function to fit a generalized ordered probit model that regresses original self-reported status measures on two sets of independent variables (King et al. 2004; Jürges 2007; Oksuzyan et al. 2019). The first set of variables (e.g., health variables) included in the regression are individual statuses and characteristics that are directly related to the self-reported variable. In the case of self-reported health, these could be chronic conditions, mobility level, difficulties with daily activities, performance on grip strength tests, anthropometric measures, and lifestyle behaviors. The second set of independent variables (threshold variables) is used to model cut-points between adjacent self-reported response categories as functions of individual characteristics, such as gender, age group, education, and country (Oksuzyan et al. 2019). The model helps to adjust for specific socio-demographic and cultural differences in how the continuous latent health is projected onto the ordinal self-rated measure. The fitted model can be used to calculate an individual predicted latent status variable, a latent index, and standardized latent coefficients; and makes it possible to reclassify a categorical status measure that has been adjusted for inter-individual differences in reporting behavior.

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# 1 Introduction

**hopit** is an open source software library written in the R (R-Core-Team 2018) and C++ (Bates and Eddelbuettel 2013; Eddelbuettel and François 2011) programming languages. The **hopit** package provides versatile methods for fitting and analyzing ordered response data to adjust for heterogeneity in reporting behavior.

The ordered response data classify a measure of interest into ordered categories provided as a response option for a question asked during a survey. If, for example, the dependent variable is a happiness rating, then a respondent typically answers a question such as: "Taking all things together, would you say you are ... ?"; and then selects from response options such as: "very happy", "pretty happy", "not too happy", and "very unhappy" (Liao, Fu, and Yi 2005). Similarly, if interviewees are asked to evaluate their general health (e.g., "Would you say your health is ... ?"), they may choose among several categories, such as "very good", "good", "fair", "bad", and "very bad" (King et al. 2004; Jürges 2007; Rebelo and Pereira 2014; Oksuzyan et al. 2019). In political science, respondents may be asked for their opinions about recent legislation (e.g., "Rate your feelings about the proposed legislation."), and instructed to choose among categories like "strongly oppose", "mildly oppose", "indifferent", "mildly support", and "strongly support" (Greene and Hensher 2010). It is easy to imagine other multi-level ordinal variables that might be used in a survey, and to which the methodology described below could be applied.

In practice, it is assumed that when responding to a survey question about their general happiness, health, feelings, attitudes, or other status, participants are assessing the true value of this unobserved continuous variable, and project it onto the discrete scale provided. The thresholds that different individuals use to categorize their true status by selecting a specific response option may be affected by the reference group chosen, their earlier life experiences, and cross-cultural differences in the use of such scales. Thus, the responses of individuals may vary depending on their gender, age, cultural background, education, and personality traits; among other factors.

From the perspective of reporting behavior modeling, among the main tasks researchers face are computing this continuous estimate of the underlying, latent measure for each individual based on several specific characteristics of the responses considered, and accounting for variations in reporting across socio-demographic and cultural groups. More specifically, to build a latent, underlying measure, a generalized hierarchical ordered threshold model is fitted that regresses the reported status/attitude/feeling on two sets of independent variables (Boes and Winkelmann 2006; Greene et al. 2014). When the dependent reported ordered variable is self-rated health status, then the first set of variables - i.e., health variables - assess specific aspects of individuals' health, such as measures of chronic conditions, mobility, difficulties with a range of daily activities, grip strength, anthropometric characteristics, and lifestyle behaviors. Using the second set of independent variables (threshold variables), the model also adjusts for differences across socio-demographic and cultural groups. It allows the threshold between adjacent response categories to differ among individuals of different ages, genders, educational levels, and cultural backgrounds. (King et al. 2004; Jürges 2007; Oksuzyan et al. 2019; but see Rebelo and Pereira 2014).

Once the model is fitted, its estimates (latent measure and threshold coefficients) can be used to calculate the differences in reporting behavior among groups of people with different contextual characteristics through the calculation of differences between the expected and the reported ordinal response measures (Jürges 2007; Oksuzyan et al. 2019).

# 2 Methods

#### Table 1. Glossary.

Term	Symbol	Definition	Exemplary case specific synonyms
Categorical response	y	Dependent variable obtained during the survey	Self-rated health, self-rated happiness
Latent measure	h	Modeled continuous latent measure of the investigated response variable	Latent health, latent happiness
Latent index	Н	Standardized latent measure	Health index, happiness index
Latent variables		Variables used to model the latent measure	Health variables, happiness variables
Latent terms	X	Terms of the design matrix used to model the latent measure	
Latent coefficients	eta	Coefficients corresponding to each latent term	
Standardized coefficient	D	Standardized value of a coefficient	Disability weights
Thresholds	$\alpha$	Thresholds used to group the latent measure	Cut-points
Threshold variables		Variables used to model the thresholds	Socio-demographic, cultural, contextual variables
Threshold terms	Y	Terms of the design matrix used to model the latent measure	
Threshold coefficients	$\gamma,\lambda$	Coefficients corresponding to each threshold term	

## 2.1 Generalized (hierarchical) ordered threshold model

Ordered threshold models are used to fit ordered categorical dependent variables. The generalized ordered threshold models (Ierza 1985; Boes and Winkelmann 2006; Greene et al. 2014) are an extension of ordered threshold models (McKelvey and Zavoina 1975). Whereas in the latter models the thresholds are constant, in the generalized models the thresholds are allowed to be dependent on covariates. Greene and Hensher (2010) and Greene et al. (2014) pointed out that for a model to make sense, the thresholds must also be ordered. This observation motivated Greene and coauthors to call these models *HOPIT*, which stands for hierarchical ordered probit models.

In the self-rated health example, the response variable is self-rated health, and the latent measure  $h_i$  can depend on different health conditions and diseases (health variables). These variables are

modeled with the parallel regression assumption. According to this assumption, the coefficients that describe the relationship between the lowest response category and all of the higher response categories are the same as the coefficients that describe the relationship between another (e.g., adjacent) lowest response category and the remaining higher response categories. In the considered case,  $h_i$  is modeled as a linear function of the design matrix of health variables X and its corresponding coefficients  $\beta$ :

$$h_i = \sum_{k=1}^K \beta_k X_{i,k} = X'\beta \tag{1}$$

where index  $i \in 1...N$  is a number of cases (e.g., respondents), X is in the form of a design matrix, and K is the number of columns in X. As described above, the categorization (response mechanism) of the latent measure  $h_i$  is modeled in terms of thresholds  $\alpha_{i,j}$ , while assuming that the lower order thresholds are never greater than the higher order thresholds (hierarchical assumption):

$$\begin{cases} y_i = 1 \iff \alpha_{i,0} \le h_i < \alpha_{i,1} \\ y_i = 2 \iff \alpha_{i,1} \le h_i < \alpha_{i,2} \\ \cdots \\ y_i = j \iff \alpha_{i,j-1} \le h_i < \alpha_{i,j} \\ \cdots \\ y_i = J \iff \alpha_{i,J-1} \le h_i < \alpha_{i,J} \end{cases}$$

$$(2)$$

The thresholds (cut-points,  $\alpha$ ) are modeled using threshold variables coded as design matrix Y, their coefficients  $\gamma$ , and intercepts  $\lambda$ . These variables model the contextual characteristics of the respondent (e.g., country, gender, and age). As the threshold variables are modeled without applying the parallel regression assumption, each threshold is modeled by a variable separately (Boes and Winkelmann 2006; Greene et al. 2014).

Different parametrizations of thresholds exist (Greene et al. 2014; Rebelo and Pereira 2014; Jürges 2007). In the package, the parametrization of King et al. (2004) and Jürges (2007) is used, which assumes that:

$$\alpha_{i, j} = \begin{cases} -\infty & for \ j = 0\\ \lambda_1 + \sum_{m=1}^{M} \gamma_{1,m} Y_{i,m} & for \ j = 1\\ \alpha_{i, j-1} + exp(\lambda_j + \sum_{m=1}^{M} \gamma_{j,m} Y_{i,m}) & for \ J - 1 \ge j \ge 2\\ \infty & for \ j = J \end{cases}$$
(3)

The condition  $y_i = j \iff \alpha_{j-1,i} \le h_i < \alpha_{j,i}$  can be easily expressed in terms of the probability, which leads to:

$$P(y_i = j) = P(\alpha_{j-1,i} \le h_i < \alpha_{j,i}), \tag{4}$$

hence

$$P(y_i = j) = \Phi(\alpha_{i, j} - h_i) - \Phi(\alpha_{i, j-1} - h_i),$$
(5)

where  $\Phi$  is a distribution function (cdf, cumulative density function). For example, for probit regression it is standard normal cdf  $\Phi(x) = \frac{1}{2} + \frac{1}{2} * erf\left(\frac{x}{\sqrt{2}}\right)$ , whereas for logit regression it takes

the form  $\Phi(x) = \frac{1}{1+e^{-x}}$ . In reporting behavior analyses the probit model is typically chosen. This model simply assumes that  $h_i$  is affected by a random noise  $\epsilon_i$  having standard normal distribution  $\epsilon_i \sim \mathcal{N}(0, 1)$ .

Using all of the definitions presented above, the log likelihood function can be constructed as:

$$\ln L = \sum_{i=1}^{N} \sum_{j=1}^{J} z_{i, j} \ln \left[ \Phi(\alpha_{i, j} - h_i) - \Phi(\alpha_{i, j-1} - h_i) \right], \tag{6}$$

where  $z_{i,j}$  is an indicator function defined as:

$$z_{i, j} = \begin{cases} 0 & \text{for } y_i = j \\ 1 & \text{for } y_i \neq j \end{cases}$$

$$\tag{7}$$

#### 2.2 Analysis of reporting heterogeneity

The model estimates are used to determine reporting behavior; i.e., how the continuous latent measure is projected onto the categorical response. In practice, this is done by comparing actual categorical ordered responses with theoretical responses that are adjusted for heterogeneity in reporting behaviors, and are, therefore, more comparable across individuals.

One of the first steps of the analysis is the standardization of the latent measure to obtain the latent index  $H_i$ .

$$H_i = 1 - \frac{h_i - \min_i h_i}{\max_i h_i - \min_i h_i}$$

$$\tag{8}$$

In the self-rated health example,  $H_i$  is a proxy for the true underlying health of an individual, and varies from 0, representing the (model-based) worst health state in the sample, to 1, representing the (model-based) best health state in the sample.

The predicted latent measure  $h_i$  obtained from the model is also used to standardize the latent variable coefficients. In the self-rated health example, the standardized coefficients are called disability weights  $D_k$  (Jürges 2007; Oksuzyan et al. 2019) and are calculated for each health variable to provide information about the impact of a specific health measure on the latent index  $H_i$ . The disability weight for a health variable is equal to the ratio of the corresponding health coefficient and the difference between the lowest and the highest values of predicted latent health. In other words, the disability weight reduces  $H_i$  by some given amount or percentage (i.e., the  $H_i$  of each individual is reduced by the same amount if the person had a heart attack or other heart problems)(Jürges 2007; Oksuzyan et al. 2019).

$$D_k = \frac{\beta_k}{\max_i h_i - \min_i h_i} \tag{9}$$

While the latent index  $H_i$  is intended to reflect the underlying health, happiness, or other status across individuals, the standardized coefficients  $D_k$  (e.g., disability weights in the case of self-rated health) are computed for an average individual in the study population. The relationship between  $H_i$  and  $D_k$  follows the equation:

$$H_i = C - \sum_{k=1}^K D_k X_{i,k}, \quad \text{where } C = \frac{\max_i h_i}{\max_i h_i - \min_i h_i}$$
(10)

Reporting behavior analysis is based on the reclassification of individuals into new response categories. There are two methods of reclassification: (1) the Jürges (2007) percentile method (see also Rebelo and Pereira 2014; Oksuzyan et al. 2019) and (2) the direct reclassification method based on model-estimated thresholds.

In the first method, the classification is based on the calculated latent index  $H_i$ , which is adjusted for inter-individual differences in reporting behavior. This method is based on the original distribution of the categorical response variable (see also 4.2). First, for each category j, an empirical distribution function is constructed:

$$\hat{F}(j) = \frac{1}{N} \sum_{i=1}^{N} \mathbf{1}_{y_i} \le j$$

$$\tag{11}$$

where **1** is an indicator function taking 1 if the condition is true, or is 0 otherwise. The calculated cumulative frequencies of the latent index  $H_i$  are used as percentiles (cut-points) so that each individual *i* can be reclassified into a new response category.

In the second method the reclassification is based on eq. (2), so that each individual has her/his own model-derived cut-points.

# 3 Fitting the model to the exemplary health survey data using the hopit package

#### 3.1 Installing and loading the package

To install and load the package simply run the following code:

```
install.packages("hopit")
```

library(hopit)

#### 3.2 Exemplary data

In the examples presented below I use healthsurvey, which is a completely artificial data set that is simulated using the distributions of some major health and socio-demographic characteristics. The distributions and the data structure are roughly based on the WAVE1 SHARE database (DOIs: 10.6103/SHARE.w1.600); see Börsch-Supan et al. (2013) for technical details about the SHARE database. The structure of healthsurvey for the first six individuals (IDs) is presented below.

print(t(healthsurvey[1:6,-1]), quote=FALSE, na.print='NA', right=TRUE)

	1	2	3	4	5	6
health	Very good	Good	Good	Good	Excellent	Good
diabetes	no	no	yes	no	no	no
obese	no	no	no	no	no	no
IADL_problems	no	no	no	no	no	no
hypertension	no	yes	no	no	no	yes
high_cholesterol	no	yes	no	no	no	yes
respiratory_problems	no	no	no	no	no	yes
$heart_attack_or_stroke$	no	yes	no	no	no	no
poor_mobility	no	no	no	no	no	yes
very_poor_grip	no	no	no	no	no	no
depression	no	no	no	yes	no	no
other_diseases	yes	yes	no	no	no	yes
sex	man	man	man	man	woman	man
ageclass	80+	70-79	50-59	60-69	80+	80+
education	prim-	prim-	prim-	sec+	prim-	prim-
country	Y	Y	Х	Y	Z	Y
CSW	2407.48	1198.12	885.26	772.04	1304.24	917.16
psu	YB	YB	XC	YA	ZB	YD

The first variable on the list (health) is the categorical self-reported health status. This variable is followed by 11 determinants of health, which include information on the presence of chronic diseases and other health conditions. The sex, ageclass, education, and country variables describe the contextual characteristics of individuals. The last group of variables (csw, psu, and ssu) describes the survey design.

## 3.3 Fitting a basic model

The generalized ordered probit models can be fitted using the hopit function. The function takes two kinds of formulas: (1) latent.formula, which models the impact of the latent variables on categorical health; and (2) thresh.formula, which models the thresholds.

One of the crucial steps needed for the proper interpretation of the model results is determining the order of the dependent variable, which must be a factor.

levels(healthsurvey\$health)

[1] "Excellent" "Very good" "Good" "Fair" "Poor"

To fit the model, the hopit function is called. Because the order is decreasing (from the best to the worst health state), the hopit parameter decreasing.levels is set to TRUE.

```
depression +
    respiratory_problems +
    IADL_problems +
    obese +
    diabetes +
    other_diseases,
thresh.formula = ~ sex + ageclass,
decreasing.levels = TRUE,
data = healthsurvey)
```

The summary of the fitted model can be created using a standard generic function.

summary(model1)

```
Formula (latent variables):
health ~ hypertension + high_cholesterol + heart_attack_or_stroke +
   poor_mobility + very_poor_grip + depression + respiratory_problems +
    IADL_problems + obese + diabetes + other_diseases
Formula (threshold variables): ~sex + ageclass
Link: probit
Number of cases: 10000
Response levels: Excellent, Very good, Good, Fair, Poor
Robust SE were used (sandwich estimator of the variance-covariance matrix).
                         Estimate Std. Error z value Pr(|z|)
hypertensionyes
                          0.19232
                                     0.02478
                                                7.76 8.4e-15 ***
                                                3.35 0.00080 ***
high cholesterolyes
                          0.09780
                                     0.02918
heart_attack_or_strokeyes 0.34401
                                     0.03183 10.81 < 2e-16 ***
                                              20.44 < 2e-16 ***
poor_mobilityyes
                          0.72832
                                     0.03564
very_poor_gripyes
                          0.49720
                                     0.12299
                                              4.04 5.3e-05 ***
depressionyes
                          0.25323
                                     0.02390
                                               10.59 < 2e-16 ***
respiratory_problemsyes
                                     0.03337
                                               11.02 < 2e-16 ***
                          0.36777
IADL problemsyes
                                              16.93 < 2e-16 ***
                                     0.03637
                          0.61579
                                              5.76 8.3e-09 ***
obeseyes
                          0.18991
                                     0.03295
                                     0.04010
                                              8.41 < 2e-16 ***
diabetesyes
                          0.33726
                                               14.15 < 2e-16 ***
other_diseasesyes
                          0.33533
                                     0.02370
(L).1|2
                         -0.09248
                                     0.03194
                                               -2.90 0.00379 **
(L).2|3
                                               -8.29 < 2e-16 ***
                         -0.26826
                                     0.03236
(L).3|4
                                               2.59 0.00968 **
                          0.07514
                                     0.02905
(L).4|5
                                              -3.90 9.8e-05 ***
                         -0.20346
                                     0.05222
(G).sexwoman.1|2
                                               0.79 0.43111
                          0.02373
                                     0.03015
(G).sexwoman.2|3
                                                0.39 0.69304
                          0.01366
                                     0.03460
(G).sexwoman.3|4
                                                1.28 0.20193
                          0.03661
                                     0.02869
(G).sexwoman.4|5
                          0.11847
                                     0.05039
                                                2.35 0.01872 *
(G).ageclass60-69.1|2
                         -0.01835
                                     0.03383
                                               -0.54 0.58763
(G).ageclass60-69.2|3
                          0.05336
                                     0.04068
                                               1.31 0.18963
```

```
(G).ageclass60-69.3|4
                           0.06003
                                      0.03616
                                                 1.66 0.09693 .
                                      0.06492
(G).ageclass60-69.4|5
                                                 2.59 0.00949 **
                           0.16842
(G).ageclass70-79.1|2
                          -0.32157
                                      0.04391
                                                -7.32 2.4e-13 ***
(G).ageclass70-79.2|3
                                      0.04774
                                                 3.59 0.00033 ***
                           0.17131
(G).ageclass70-79.3|4
                                                 5.13 3.0e-07 ***
                           0.19360
                                      0.03777
(G).ageclass70-79.4|5
                           0.23235
                                                 3.49 0.00048 ***
                                      0.06653
(G).ageclass80+.1|2
                          -0.33134
                                      0.07274
                                                -4.56 5.2e-06 ***
(G).ageclass80+.2|3
                           0.14976
                                      0.07590
                                                 1.97 0.04848 *
(G).ageclass80+.3|4
                           0.17851
                                                 3.55 0.00038 ***
                                      0.05025
(G).ageclass80+.4|5
                           0.22379
                                      0.07674
                                                 2.92 0.00354 **
___
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Sigma: 1
Log-likelihood: -12945.98
Deviance: 25891.96
AIC: 25953.96
```

model1 contains 11 dichotomous health variables and two threshold variables. The fitted coefficient includes  $\beta$  (latent.params, first 11 coefficients in the summary),  $\lambda$  (thresh.lambda, threshold intercepts, "(L)" prefix in the summary), and  $\gamma$  (thresh.gamma, parameters related to threshold covariates, "(G)" prefix in the summary). The model coefficients can be accessed directly by the generic coef(model1, aslist = TRUE) function, which has an option to group parameters into a list (aslist = TRUE); or simply by calling model1\$coef.ls.

#### 3.4 Model selection and latent-threshold interactions

model1 can be further extended by adding the country of origin to the threshold formula to control for cultural and linguistic differences.

The fit of the two models can be compared using the AIC function:

AIC(model2, model1)

model2 model1 25154.19 25953.96

or using the Likelihood Ratio Test (LRT), because the models are nested:

print(anova(model2, model1), short = TRUE)

```
Likelihood ratio test:

Chi^2 df Pr(>Chi^2)

815.78 8 <2e-16 ***

---

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

In the code above, the option short = TRUE is used to generate a shortened summary of the test. The results of LRT show that model2 is more parsimonious than model1.

While both latent.formula and thresh.formula allow the user to specify the interactions within the formulas, the interactions between latent and threshold variables can also be modeled. Depending on how an interaction is interpreted, it can be added to either the latent or the threshold formula:

```
model3 <- hopit(latent.formula = health ~ hypertension +</pre>
                      high cholesterol +
                      heart_attack_or_stroke +
                       poor_mobility +
                       very_poor_grip +
                       depression +
                       respiratory_problems +
                       IADL_problems +
                       obese +
                       diabetes +
                       other_diseases +
                       sex : respiratory_problems,
               thresh.formula = ~ sex +
                       ageclass +
                       country +
                       sex : depression,
               decreasing.levels = TRUE,
               data = healthsurvey)
```

There are two additional interactions sex : respiratory\_problems and sex : depression in model3. The first interaction has an impact on the latent health variable; i.e., respiratory\_problems has a gender-specific effect on this variable. In other words, respiratory problems (if present) affect the health of men and women differently. The second interaction modulates the effect of the gender variable on the thresholds if depression is present; i.e., women with depression have different thresholds than women without depression.

## 3.5 Including a survey design

The hopit function also has an option to include a survey design using the **survey** package (Lumley 2004, 2019). The example below fits a model using a simple two-level cluster sampling design.

```
design <- svydesign(ids = ~ country + psu, weights = healthsurvey$csw,
                    data = healthsurvey)
model2s <- hopit(latent.formula = health ~ hypertension +</pre>
                       high_cholesterol +
                       heart_attack_or_stroke +
                       poor_mobility +
                       very_poor_grip +
                       depression +
                       respiratory_problems +
                       IADL problems +
                       obese +
                       diabetes +
                       other_diseases,
                thresh.formula = ~ sex + ageclass + country,
                decreasing.levels = TRUE,
                design = design,
                data = healthsurvey)
```

Generally, ignoring the survey design can lead to biased results. However, in the example presented here, the design is of little importance. This becomes clear when comparing the coefficients of the latent variable for the two models:

	No	survey	design	Has	survey	design
hypertensionyes			0.1848			0.1841
high_cholesterolyes			0.0897			0.0830
heart_attack_or_strokeyes			0.3466			0.3504
poor_mobilityyes			0.7035			0.7019
very_poor_gripyes			0.5142			0.4982
depressionyes			0.2500			0.2527
respiratory_problemsyes			0.3786			0.3756
IADL_problemsyes			0.5926			0.5661
obeseyes			0.1904			0.1912
diabetesyes			0.3284			0.3348
other_diseasesyes			0.3294			0.3294

## 3.6 Checking the convergence of the fitted model

The accuracy of the model fit can be assessed using the **profile** function, which calculates and plots the profile of the log likelihood function around fitted coefficient values.



Figure 1: Log likelihood profile of the fitted model

It then becomes clear that the model converged to the maximum log likelihood (Fig. 1).

# 4 Analysis of reporting heterogeneity for the health data example

## 4.1 Disability weights and latent index

The fitted model can be further used to analyze reporting heterogeneity. Let us ignore latentthreshold interactions for the sake of simplicity, and consider model2 for further analyses. The latent health variables can be directly accessed using model2\$coef.ls\$latent.params. We can, however, standardize these coefficients using Jürges' approach (Jürges 2007) in order to obtain so called disability weights. The disability weights are the same for each individual in the modeled population. The standardization is done using the standardizeCoef function.

```
txtfun <- function(x) gsub('_',' ',substr(x, 1, nchar(x)-3))
sc <- standardizeCoef(model1, namesf = txtfun)</pre>
```

The namesf argument is a function or a character vector that is used to rename the coefficients. The exact values of disability weights are stored in sc:

print(sc)

	Std.	coef
hypertension	0.053	36
high cholesterol	0.027	72
heart attack or stroke	0.095	58
poor mobility	0.202	28
very poor grip	0.138	35
depression	0.070	)5
respiratory problems	0.102	24
IADL problems	0.171	5
obese	0.052	29
diabetes	0.093	39
other diseases	0.093	34

and can be summarized and plotted by the standard generic functions.

print(summary(sc), show.coef.names=FALSE)

	Standardized	coeficient	Pr( z )	
hypertension		0.0536	0.0000	***
high cholesterol		0.0272	0.0008	***
heart attack or stroke		0.0958	0.0000	***
poor mobility		0.2028	0.0000	***
very poor grip		0.1385	0.0001	***
depression		0.0705	0.0000	***
respiratory problems		0.1024	0.0000	***
IADL problems		0.1715	0.0000	***
obese		0.0529	0.0000	***

```
diabetes 0.0939 0.0000 ***
other diseases 0.0934 0.0000 ***
---
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

plot(sc)



Figure 2: Disability weights

The standardized health status for each individual is called the health index (or the latent index). It is simply calculated using the latentIndex function.

#### hi <- latentIndex(model2)</pre>

summary(hi)

The generic functions print, summary, and plot also apply here.

```
(0,0.05] (0.05,0.1] (0.1,0.15] (0.15,0.2] (0.2,0.25] (0.25,0.3] (0.3,0.35]
                      8
                                  8
                                                         50
                                                                     71
         0
                                             22
                                                                                  84
(0.35, 0.4] (0.4, 0.45]
                        (0.45, 0.5]
                                    (0.5, 0.55]
                                                (0.55, 0.6]
                                                            (0.6, 0.65]
                                                                         (0.65, 0.7]
       162
                   215
                                303
                                            310
                                                        221
                                                                    413
                                                                                 407
(0.7,0.75] (0.75,0.8] (0.8,0.85] (0.85,0.9] (0.9,0.95]
                                                               (0.95, 1]
       779
                   715
                               1410
                                           1140
                                                       2567
                                                                   1113
```





Figure 3: Health index vs. self-reported health

The boxplot above (Fig. 3) shows the reported health status versus the health index. It is also possible to plot the expected categorical health status on the Y axis, calculated according to eq. (2), by setting response = "fitted".

## 4.2 Cut-points and adjusted health levels

The main aim of the reporting heterogeneity analyses is to determine the cut-points used to calculate the adjusted health status for each individual. The calculation of cut-points is realized using the getCutPoints function.

```
z <- getCutPoints(model = model2)
plot(z)</pre>
```



Figure 4: Health index cut-points for adjusted health levels

Returned cut-points:

round(z\$cutpoints, 4)

4.41% 17.68% 52.34% 77.63% 0.4147 0.6366 0.8527 0.9067

The function also returns adjusted health levels for each individual that are calculated according the Jürges (2007) method:

rev(table(z\$adjusted.levels))

Excellent	Very good	d Good	Fair	Poor
1897	280	3499	1339	459

It is, however, also possible to obtain adjusted health levels for each individual using estimated model thresholds:

table(model2\$Ey\_i)

Excellent	Very good	Good	Fair	Poor
637	4472	4011	818	62

The analysis of health level frequencies is performed using the getLevels function:



Figure 5: Adjusted and original health levels

The formula describes the grouping variables. It is set to the threshold formula by default, but it can be changed. Here, the country variable is omitted, which means that the age-gender-specific frequencies are calculated for the combined countries. The results are plotted using the generic plot function (Fig. 5). If the model includes a survey design and weight.original = TRUE then the original frequencies are adjusted with the survey weights. The differences between the original and the adjusted frequencies (%) can be calculated directly using the getLevels output:

	Poor	Fair	Good	Very good	Excellent
man 50-59	3.28	4.77	-1.03	-9.54	2.53
woman 50-59	0.68	-1.21	-2.96	2.71	0.78
man 60-69	1.66	0.83	-3.00	-9.00	9.51
woman 60-69	0.06	-0.75	-1.18	-2.12	3.99
man 70-79	-0.19	-0.96	2.78	-2.59	0.96
woman 70-79	-3.75	-4.03	3.47	1.97	2.34
man 80+	-1.87	-6.07	5.84	-5.14	7.24
woman 80+	-13.55	1.64	4.31	7.39	0.21

#### 4.3 Bootstrapping the confidence intervals

The package offers the **boot\_hopit** and **percentile\_CI** functions for calculating the confidence intervals for any measure derived from the model using parametric bootstrap methods. In each of the bootstrap repetitions, a new set of model coefficients is drawn from the multivariate normal distribution, taking the originally estimated model coefficients as a mean, and using the model estimated variance-covariance matrix. The drawn coefficients are then used to calculate the measure of interest via a user-defined function. In the example below, I calculate the confidence intervals of the difference between the original and the adjusted frequencies of bad health. The bad health is determined by the presence of "**Poor**" or "**Fair**" self-rated health categories.

First, a function to be bootstrapped is defined, which is then used to calculate the mentioned difference:

```
diff_BadHealth <- function(model) {
    hl <- getLevels(model = model, formula = ~ sex + ageclass, sep = ' ')
    hl$original[,1] + hl$original[,2] - hl$adjusted[,1] - hl$adjusted[,2]
}</pre>
```

The function is used in the boot\_hopit function, which also needs to specify a fitted model and the data used to fit model2

```
B <- boot_hopit(model = model2, func = diff_BadHealth, nboot = 100)</pre>
```

The confidence intervals are calculated using the percentile\_CI

est.CI <- percentile\_CI(B)</pre>

The same function is used to calculate the difference based on the estimates of the model.

est.org <- diff\_BadHealth(model = model2)</pre>

The code below plots the differences and the bootstrapped confidence intervals

```
pmar <- par('mar'); par(mar = c(9.5, 6, pmar[3:4]))
m <- max(abs(est.CI))
pos <- barplot(est.org, names.arg = names(est.org), las = 3,
  ylab = 'Original - adjusted differences \nin the prevalences of bad health (%)',
  ylim = c(-m, m), density = 20, angle = c(45, -45), col = c('blue', 'orange'))
for (k in seq_along(pos))
  lines(c(pos[k,1],pos[k,1]), est.CI[,k], lwd = 2, col = 2)
abline(h = 0); box(); par(mar = pmar)</pre>
```



Figure 6: Difference between the original and the adjusted prevalences of bad health. The confidence intervals were calculated using the percentile bootstrap method.

The results (Fig. 6) show that men tend to over-report bad health at ages (50,60] and (50,70], whereas women tend to over-report bad health at ages (70,80); and that both sexes tend to underreport bad health at ages (80, 120]. See also Oksuzyan et al. (2019) for similar analyses that were performed using real SHARE data.

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